

## Hints & Solutions

### Chemistry

#### PART – A

1. A (Concept Code: C120608)

Sol. For I.  $i = 1 - \alpha + \frac{\alpha}{2}$

$$1 - \frac{\alpha}{2} = 1 - \frac{1}{2} = 0.5$$

$$\pi = iCRT = 0.5 \times 2RT$$

$$\text{II. } i = 1 + \alpha = 2$$

$$\pi = 2 \times 0.5 \times RT$$

So both are isotonic

2. C (Concept Code: C111903)

Sol.  $\Delta H_{\text{neutralization}} = \Delta H_{\text{n(SA/SB)}} + \Delta H_{\text{i}}$

$$-13.2 = -13.7 + \Delta H_{\text{ionization}}$$

$$\Delta H_{\text{ionization}} = 0.5 \text{ or } 5 \times 10^{-1}$$

3. D (Concept Code: C120207)

Sol.  $\text{HgCl}_2$  is covalent halide.

4. C (Concept Code: C120205)

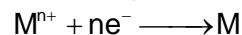
Sol. AgBr shows both Schottky and Frenkel defect.

5. ABCD (Concept Code: C120601)

Sol. based on Raoult's law  $P_{\text{T}} = P_{\text{A}}^0 X_{\text{A}}^0 + P_{\text{B}}^0 X_{\text{B}}^0$

6. ABC (Concept Code: C120504)

Sol. Nernst equation for half-cell reaction



$$E_{\text{red}} = E_{\text{red}}^{\circ} - \frac{2.303RT}{nF} \log \frac{1}{[\text{M}^{n+}]}$$

On addition of  $\text{CN}^-$  ( $\text{AgCN}$  ppt and  $\text{Ag}^+$  conc. dec)

7. ABCD (Concept Code: C120308)

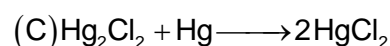
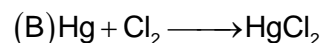
Sol. Fact based.

8. ACD (Concept Code: C110504)

Sol. Except B (Strong base + salt of strong acid & strong base) all are buffer (weak acid + salt of weak acid & strong base).

9. ABC (Concept Code: C120201)

Sol. (A)  $3\text{HgS} + 6\text{HCl} + 2\text{HNO}_3 \longrightarrow 3\text{HgCl}_2 + 3\text{S} + 4\text{H}_2$



10. AC (Concept Code: C113616)

Sol. Si has vacant d-orbitals and lone pairs over nitrogen is involved in back bonding ( $d\pi - p\pi$ ).

**PART – B**

1. **A → PQT                      B → PST                      C → RS                      D → P**  
 (Concept Code: C124602, C121402, C122833)

2. **A → PR                      B → Q                      C → Q                      D → S** (Concept Code: C123201)

Sol. A → PR : for reversible isothermal process

$$W = 2.303nRT \log \frac{V_2}{V_1} = 2.303 nRT \log \frac{P_1}{P_2}$$

B → Q : for adiabatic process  $PV^\gamma = \text{constant}$

C → Q :  $W = \frac{nR}{\gamma - 1} (T_2 - T_1)$  for adiabatic process also  $PV^\gamma = \text{constant}$

D → S : Irreversible isothermal process

3. **A → Q                      B → R                      C → S                      D → Q** (Concept Code: C120609)

Sol. A →  $i = 1 + \alpha = 2 \Rightarrow \Delta T_b = iK_b = 2K_b$

B →  $i = 1 + 2 \times 0.75 = 2.5 \quad \Delta T_b = 2.5 K_b$

C →  $i = 1 + 4 \times 0.5 = 3 \quad \Delta T_b = 3 K_b$

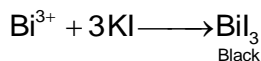
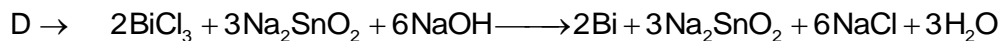
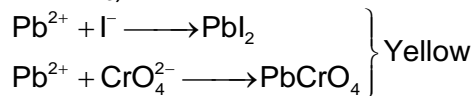
D →  $i = 1 + 4 \times 0.25 = 2 \quad \Delta T_b = 2 K_b$

4. **A → T                      B → R                      C → PS                      D → PQ** (Concept Code: C120201)

Sol. A → T

B → (These dissolve as soluble nitrate in 50% HNO<sub>3</sub>)

C → (50% HNO<sub>3</sub>)



**PART – C**

1. 0 (Concept Code: C123204)

Sol. For isothermal reversible process

$$\Delta S_{\text{universe}} = \Delta S_{\text{system}} + \Delta S_{\text{surrounding}} = \frac{q_{\text{rev}}}{T} - \frac{q_{\text{rev}}}{T} = 0$$

2. 2 (Concept Code: C120504)

Sol.  $E_{\text{Cell}} = \frac{0.0591}{n} \log \frac{0.1 \times 10^{-x}}{10^{-11}}$

$$0.48 = \frac{0.0591}{1} \log 10^{10-x}$$

Solving  $x = 2$

3. 6 (Concept Code: C120201)

Sol. Black coloured sulphides (PbS, CuS, HgS & Ag<sub>2</sub>S, NiS, CoS)

4. 3 (Concept Code: C120308)

Sol. C.No. 12, No. of atoms = 4

$$\text{Ratio} = \frac{12}{4} = 3$$

5. 3 (Concept Code: C121701)

Sol. Buna-S, Nylon-2-Nylon-6, Bakelite are co-polymers



6. 2 (Concept Code: C120609)

Sol.  $\pi = iCRT$

$$2.69 = i \times 0.1 \times 0.082 \times 298$$

$$i = 1.1$$

For monobasic acid  $HA \rightleftharpoons H^+ + A^-$

$$i = 1 + \alpha$$

$$\alpha = 0.1$$

$$\text{So } [H^+] = C \alpha = 0.1 \times 0.1 = 10^{-2}$$

$$\therefore \text{pH} = -\log(10^{-2}) = 2$$

### Mathematics

#### PART – A

1. Any point on the given parabola is  $(t^2, 2t)$ . The equation of the tangent at  $(1, 2)$  is

$$x - y + 1 = 0.$$

The image  $(h, k)$  of the point  $(t^2, 2t)$  in  $x - y + 1 = 0$  is given by  $\frac{h - t^2}{1} = \frac{k - 2t}{-1} = \frac{-2(t^2 - 2t + 1)}{1 + 1}$

$$\therefore h = t^2 - t^2 + 2t - 1 = 2t - 1$$

$$\text{and } k = 2t + t^2 - 2t + 1 = t^2 + 1$$

Eliminating  $t$  from  $h = 2t - 1$  and  $k = t^2 + 1$

$$\text{We get, } (h + 1)^2 = 4(k - 1)$$

The required equation of reflection is  $(x + 1)^2 = 4(y - 1)$

2. Let  $\Delta(x) = A + Bx + Cx^2 + Dx^3 + \dots$

$$\therefore \Delta(0) = \begin{vmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{vmatrix} = 0 \Rightarrow A = 0$$

$$\Delta'(0) = \begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{vmatrix} + \begin{vmatrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{vmatrix} + \begin{vmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{vmatrix} = 1$$

$$\therefore B = 1$$

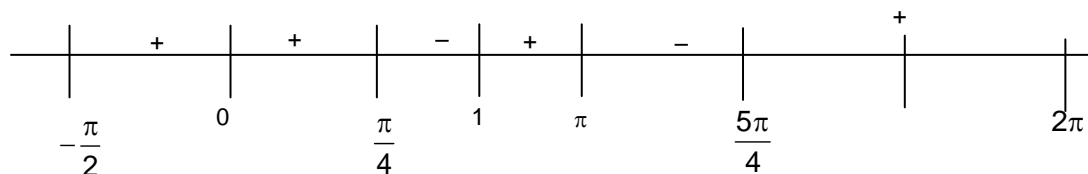
$$\Rightarrow \text{Then } \Delta(x) = x + Cx^2 + Dx^3 + \dots$$

$\therefore \Delta(x)$  is divisible by  $x$ .

3. By property,  $\text{adj } A^T - (\text{adj } A)^T = O^*$  null matrix.

4.  $f'(x) = (e^x - 1)(x - 1)(\sin x - \cos x) \sin x$

Sign scheme of  $f'(x)$  is



Clearly,  $f(x)$  is increasing in  $\left(-\frac{\pi}{2}, \frac{\pi}{4}\right) \cup (1, \pi) \cup \left(\frac{5\pi}{4}, 2\pi\right)$  and decreasing in  $\left(\frac{\pi}{4}, 1\right) \cup \left(\pi, \frac{5\pi}{4}\right)$ .

5. We have  $[\vec{p} \ \vec{q} \ \vec{r}] = \frac{1}{[\vec{a} \ \vec{b} \ \vec{c}]}$

Therefore,  $[\vec{p} \ \vec{q} \ \vec{r}] > 0$

(a)  $x > 0, x \left[ \vec{a} \ \vec{b} \ \vec{c} \right] + \frac{\left[ \vec{p} \ \vec{q} \ \vec{r} \right]}{x} \geq 2$  (Using  $AM \geq GM$ )

(b) similarly, use  $AM \geq GM$

6. We have,

$$D = (b - c)^2 - 4a(a - b - c) > 0$$

$$\Rightarrow b^2 + c^2 - 2bc - 4a^2 + 4ab + 4ac > 0$$

$$\Rightarrow c^2 + (4a - 2b)c - 4a^2 + 4ab + b^2 > 0 \text{ for all } c \in \mathbb{R}$$

Discriminant of the above expression in  $c$  must be negative.

$$\text{Hence, } (4a - 2b)^2 - 4(-4a^2 + 4ab + b^2) < 0$$

$$\Rightarrow 4a^2 - 4ab + b^2 + 4a^2 - 4ab - b^2 < 0$$

$$\Rightarrow a(a - b) < 0$$

$$\Rightarrow a < 0 \text{ and } a - b > 0 \text{ or } a > 0 \text{ and } a - b < 0$$

$$\Rightarrow b < a < 0 \text{ or } b > a > 0$$

7.  $\therefore 2 \cos \theta = x + \frac{1}{x}$

$$x^2 - 2x \cos \theta + 1 = 0$$

$$\therefore x = \frac{2 \cos \theta \pm \sqrt{(4 \cos^2 \theta - 4)}}{2} = \cos \theta \pm i \sin \theta$$

Let  $x = e^{i\theta}$

Similarly  $y = e^{i\phi}$

Alternate (A) :

$$\frac{x}{y} + \frac{y}{x} = e^{i(\theta - \phi)} + e^{-i(\theta - \phi)}$$

$$= 2 \cos(\theta - \phi)$$

Alternate (B) :

$$x^m y^n + \frac{1}{x^m y^n} = e^{i(m\theta + n\phi)} + e^{-i(m\theta + n\phi)}$$

$$= 2 \cos(m\theta + n\phi)$$

Alternate (C) :

$$\frac{x^m}{y^n} + \frac{y^n}{x^m} = e^{i(m\theta - n\phi)} + e^{-i(m\theta - n\phi)}$$

$$= 2 \cos(m\theta - n\phi)$$

Alternate (D) :

$$xy + \frac{1}{xy} = e^{i(\theta + \phi)} + e^{-i(\theta + \phi)} = 2 \cos(\theta + \phi)$$

8. Let  $\Delta = \begin{vmatrix} \sqrt{6} & 2i & 3 + \sqrt{6} \\ \sqrt{12} & \sqrt{3} + \sqrt{8}i & 3\sqrt{2} + \sqrt{6}i \\ \sqrt{18} & \sqrt{2} + \sqrt{12}i & \sqrt{27} + 2i \end{vmatrix}$

Applying  $R_2 \rightarrow R_2 - \sqrt{2}R_1$  and  $R_3 \rightarrow R_3 - \sqrt{3}R_1$

$$\therefore \Delta = \begin{vmatrix} \sqrt{6} & 2i & 3 + \sqrt{6} \\ 0 & \sqrt{3} & i\sqrt{6} - \sqrt{12} \\ 0 & \sqrt{2} & 2i - \sqrt{18} \end{vmatrix} = \sqrt{6}(-\sqrt{6})$$

$$= -6 \text{ (real and rational)}$$

9. Since the greatest integer function is discontinuous at integral values of  $x$ , then for a given limit to exist both left and right hand limit must be equal.

$$\begin{aligned} \text{L.H.L} &= \lim_{x \rightarrow 1^-} (2 - x + a[x - 1] + a[x - 1] + b[1 + x]) \\ &= 2 - 1 + a(-1) + b(1) = 1 - a + b \end{aligned}$$

$$\begin{aligned} \text{R.H.L} &= \lim_{x \rightarrow 1^+} (2 - x + a[x - 1] + b[1 + x]) \\ &= 2 - 1 + a(0) + b(2) = 1 + 2b \end{aligned}$$

On comparing we have  $-a = b$

10. Use basic properties of log.

### PART – B

1.  $F'(x) = (x - 1)(x - 2)^2$  and  $F$  is continuously differentiable throughout  $\mathbb{R}$ .  $F'(x) = 0$   
 $\Rightarrow x = 1, x = 2$ . For  $x < 1$ ,  $F'(x) < 0$  and for  $x > 1$ ,  $F'(x) > 0$ .

Hence  $x = 1$  is point of minimum. Moreover  $F$  increases on  $(1, \infty)$  and decreases on  $(-\infty, -1)$ . At  $x = 2$ ,  $F'(x)$  does not change sign, so there is no extremum at  $x = 2$ . The minimum value

$$\begin{aligned} F(1) &= \int_0^1 (t - 1)(t - 2)^2 dt = \int_{-1}^0 t(t - 1)^2 dt \\ &= \frac{-17}{12} \in (-4, -1) \end{aligned}$$

2. Putting  $V = \frac{y}{x}$ , we obtain  $V + x \frac{dV}{dx} = V + \tan V$

$$\Rightarrow \frac{dx}{x} = \cot V dV$$

Integrating  $\log x = \log \sin V + \text{Const.}$

$$\Rightarrow x = C \sin \frac{y}{x}$$

Putting  $x = 1, y = \frac{\pi}{2}$ , we have  $C = 1$

$$\text{Thus, } x = \sin \left( \frac{y}{x} \right) \Rightarrow y = x \sin^{-1} x = f(x)$$

$f$  is defined on  $[-1, 1]$  and the range of  $f$  is  $\left[ \frac{-\pi}{2}, \frac{\pi}{2} \right]$ .

Clearly,  $f$  is continuous on its domain which is  $[-1, 1]$  and  $f(x) \leq \frac{\pi}{2} < 2$  for all  $x \in [-1, 1]$

- 3.

(A)  $|\vec{a} + \vec{b}| = |\vec{a} + 2\vec{b}|$   
 $\Rightarrow a^2 + b^2 + 2\vec{a} \cdot \vec{b} = a^2 + 4b^2 + 4\vec{a} \cdot \vec{b}$   
 $\Rightarrow 2\vec{a} \cdot \vec{b} = -3b^2 < 0$

Hence, angle between  $\vec{a}$  and  $\vec{b}$  is obtuse.

(B)  $|\vec{a} + \vec{b}| = |\vec{a} - 2\vec{b}|$   
 $\Rightarrow a^2 + b^2 + 2\vec{a} \cdot \vec{b} = a^2 + 4b^2 - 4\vec{a} \cdot \vec{b}$   
 $\Rightarrow 6\vec{a} \cdot \vec{b} = 3b^2$

Hence, angle between  $\vec{a}$  and  $\vec{b}$  is acute.

(C)  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$   
 $\Rightarrow \vec{a} \cdot \vec{b} = 0$

$\Rightarrow \vec{a}$  is perpendicular to  $\vec{b}$ .

(D)  $\vec{c} \times (\vec{a} \times \vec{b})$  lies in the plane of vector  $\vec{a}$  and  $\vec{b}$ . A vector perpendicular to this plane is parallel to  $\vec{a} \times \vec{b}$ . Hence, angle is  $0^\circ$ .

4. Let  $X$  = the number of steps taken in the forward direction, then  $X \sim B(n, p)$  with  $n = 11, p = 0.4$ .

$$p_1 = P(X=5) + P(X=6)$$

$$= {}^{11}C_5 p^5 q^6 + {}^{11}C_6 p^6 q^5$$

$$= {}^{11}C_5 (pq)^5 = {}^{11}C_5 (0.24)^5$$

$$p_3 = P(X=4) + P(X=7)$$

$$= {}^{11}C_4 p^4 q^7 + {}^{11}C_7 p^7 q^4$$

$$= {}^{11}C_4 (pq)^4 (1 - 3pq)$$

$$= {}^{11}C_4 (0.24)^4 (0.28)$$

$$p_{10} = 0 \text{ and } p_{11} = P(X=0) + P(X=11)$$

$$= (0.4)^{11} + (0.6)^{11}$$

### PART – C

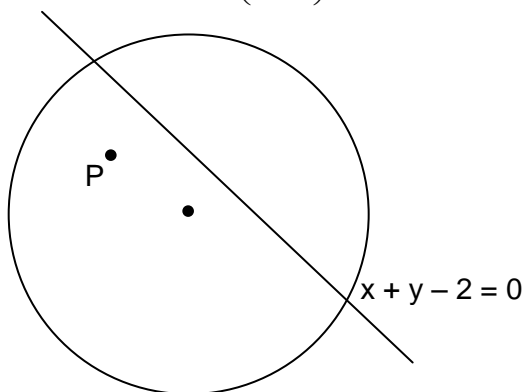
1. Let  $\frac{3iz_2}{5z_1} = k$ , where  $k \in \mathbb{R}$

$$\Rightarrow \frac{z_2}{z_1} = -\frac{5i}{3}k = ai \text{ (say)}$$

$$\text{Now, } 5 \left| \frac{3z_1 + 7z_2}{3z_1 - 7z_2} \right| = 5 \left| \frac{3 + 7ai}{3 - 7ai} \right| = 5$$

2. The given circle  $S(x, y) \equiv x^2 + y^2 - x - y - 6 = 0$  .....(i)

has centre at  $C \equiv \left( \frac{1}{2}, \frac{1}{2} \right)$



According to the required conditions, the given point  $P(\alpha - 1, \alpha + 1)$  must lie inside the given circle,

i.e.  $S(\alpha - 1, \alpha + 1) < 0$

$$\Rightarrow (\alpha - 1)^2 + (\alpha + 1)^2 - (\alpha - 1) - (\alpha + 1) - 6 < 0$$

$$\Rightarrow \alpha^2 - \alpha - 2 < 0, \text{ i.e., } (\alpha - 2)(\alpha + 1) < 0$$

$$\Rightarrow -1 < \alpha < 2 \text{ (Using sign scheme from algebra)} \quad \text{.....(ii)}$$

$$L(x, y) \equiv x + y - 2 = 0 \quad \text{.....(iii)}$$

$$\text{Since } L\left(\frac{1}{2}, \frac{1}{2}\right) = \frac{1}{2} + \frac{1}{2} - 2 < 0,$$

$$\text{i.e., } \alpha < 1 \quad \text{.....(iv)}$$

Inequalities (ii) and (iv) together give the permissible values of  $\alpha$  as  $-1 < \alpha < 1$

$$3. \quad \text{Let } f(x) + \frac{a}{30} = 0 \text{ where } f(x) = \frac{x^3 - 6x^2 + 11x - 6}{x^3 + x^2 - 10x + 8}$$

$$= \frac{(x-1)(x-2)(x-3)}{(x-1)(x-2)(x+4)}$$

$$= \frac{(x-3)}{x+4}, x \neq 1, 2, -4$$

$$\text{Range of } f(x) = \mathbb{R} - \left\{ 1, -\frac{2}{5}, -\frac{1}{6} \right\}$$

So, the equation does not have solution if

$$\frac{a}{30} = -1, \frac{2}{5}, \frac{1}{6}$$

$$\therefore a = -30, 12, 5$$

$$4. \quad \text{Let } I = \int \frac{(5x^4 + 4x^5)}{(x^5 + x + 1)^2} dx$$

Dividing above and below by  $x^{10}$ , we get

$$I = \int \frac{\left(\frac{5}{x^6} + \frac{4}{x^5}\right) dx}{\left(1 + \frac{1}{x^4} + \frac{1}{x^5}\right)^2}$$

$$\text{Putting } 1 + \frac{1}{x^4} + \frac{1}{x^5} = t,$$

$$\left(-\frac{4}{x^5} - \frac{5}{x^6}\right) dx = dt$$

$$\text{or } \left(\frac{4}{x^5} + \frac{5}{x^6}\right) dx = -dt, \text{ we get}$$

$$I = -\int \frac{dt}{t^2} = \frac{1}{t} + C = \frac{1}{\left(1 + \frac{1}{x^4} + \frac{1}{x^5}\right)} + C$$

$$= \frac{x^5}{(x^5 + x + 1)} + C$$

$$f(1) = \frac{1}{3}$$

$$5. \quad \text{Given, } y = 1 + \frac{8}{x^2}$$

Here,  $y$  is always positive. So, the curve lies above the  $x$  – axis.

$$\text{Required area} = \int_2^4 y dx = \int_2^4 \left(1 + \frac{8}{x^2}\right) dx$$

$$= \left[ x - \frac{8}{x} \right]_2^4 = 4$$

$$\text{If } x = a \text{ bisects the area, we have } \int_2^a \left(1 + \frac{8}{x^2}\right) dx = \left[ x - \frac{8}{x} \right]_2^a$$

$$= \left[ a - \frac{8}{a} - 2 + 4 \right] = \frac{4}{2}$$

$$\Rightarrow a - \frac{8}{a} = 0$$



$$\Rightarrow a^2 = 8$$

$$\Rightarrow a = \pm 2\sqrt{2}$$

Since,  $a > 2$ ,  $a = 2\sqrt{2}$ .

6. If the given points are A, B and C then  $\vec{AB} = k(\vec{BC})$

$$\Rightarrow 2\hat{i} - 8\hat{j} = k[(a - 12)\hat{i} + 16\hat{j}]$$

Comparing the coefficients of  $\hat{i}$  and  $\hat{j}$ , we get  $-8 = 16k$

$$\Rightarrow k = -\frac{1}{2}$$

$$2 = k(a - 12) = -\frac{1}{2}(a - 12)$$

$$\Rightarrow a = 8$$

### Physics PART – A

1. **D** P120409

Sol.  $m\omega^2 r = eE$

$$\Rightarrow \Delta V = \int \mathbf{E} \cdot d\mathbf{r} = \int_0^a \frac{e\omega^2 r dr}{m}$$

2. **B** P120405

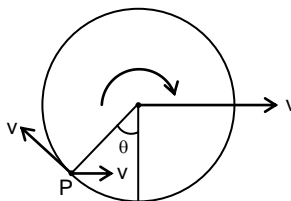
Sol.  $Q = \frac{\Delta\phi}{R}$

3. **A** P111826

Sol. Velocity of point P

$$= \sqrt{(v - v \cos\theta)^2 + (v \sin\theta)^2}$$

$$= 2v \sin\left(\frac{\theta}{2}\right)$$



4. **B** P120305

Sol.  $d = \frac{mv_0}{qB} + \frac{2mv_0}{2qB}$

5. **ABD** P111822

Sol. By conservation of angular momentum,

$$I_1\omega_i = (I_1 + I_2)\omega_f$$

$$\omega_f = \omega_i / 3$$

$$E_i = \frac{1}{2} I_1 \omega_i^2$$

$$E_f = \frac{1}{2} (I_1 + I_2) \omega_f^2$$

$$\text{Ratio of the heat produced to initial kinetic energy} = \frac{E_i - E_f}{E_i} = \frac{2}{3}$$

6. **ABD** P120406

Sol. The power delivered by magnetic field is zero. Hence, loss of energy in conducting rod is equal to heat dissipated in the resistor.

7. **ABD** P111010

Sol. Bernoulli's theorem for an orifice at depth 'x' in liquid '3d'.

$$P_o + \left( dg \frac{H}{2} + 3dg.x \right) = P_o + \frac{1}{2} \times 3d \times v^2 \quad \dots(1)$$

$$\frac{H}{2} - x = \frac{1}{2}gt^2 \quad \dots(2)$$

$$R = Vt \quad \dots(3)$$

Solve for R and apply maxima/minima.

8. **BD** P121705

Sol. At time t, the distance traveled by the rod is

$$ED = vt$$

$$\tan \alpha = \frac{AD}{ED} \text{ or } AD = ED \tan \alpha$$

$$AD = vt \tan \alpha$$

$$\tan(90 - \alpha) = \frac{DC}{ED} \text{ or } DC = at \cot \alpha$$

So,  $AC = AD + DC = vt(\tan \alpha + \cot \alpha)$

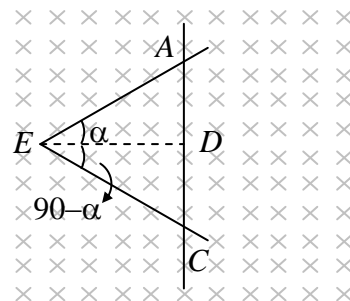
$$\text{Induced emf} = BvI = Bv(AC)$$

$$= Bv.vt(\tan \alpha + \cot \alpha)$$

$$\text{Induced emf} = Bv^2t(\tan \alpha + \cot \alpha)$$

Hence, Induced emf  $\propto t$  and  $v^2$

Therefore, choices (B) and (D) are correct and choices (A) and (C) are wrong.



9. **AC** P121720

Sol.  $I = \frac{E}{R}(1 - e^{-Rt/L})$  ;  $\frac{dI}{dt} = \frac{E}{L}(e^{-Rt/L})$

10. **BD** P120308

Sol. In both case (b) and (d),  $\vec{F}_{net} = 0$  so it passes the region undeviated.

**PART – B**

1. **A → P**                      **B → PQS**                      **C → QS**                      **D → QRS**  
P120414

2. **A → PR**                      **B → PR**                      **C → QS**                      **D → PQRS**  
P120305

Sol. Time varying magnetic field produces electric field and this electric field can apply force on a stationary charge.

3. **A → T**                      **B → S**                      **C → R**                      **D → T**  
P120216

Sol.  $q = CV - (CV - q_0) e^{-\frac{t}{CR}}$

$$i = \frac{CV - q_0}{CR} e^{-\frac{t}{CR}}$$

$$U = \frac{q^2}{2C}$$

4. **A → R**                      **B → S**                      **C → P**                      **D → Q**  
P111820

Sol. (A)  $\frac{mg}{2} \frac{\ell}{4} = T \frac{3\ell}{4} \Rightarrow T = \frac{mg}{6}$

(B)  $f_r = mg \frac{\sqrt{3}}{2}$

(C)  $N = \frac{mg}{2} \times \frac{4}{7} = \frac{2mg}{7}$

(D)  $N = \frac{mg}{2} - \frac{mg}{6} = \frac{mg}{3}$

**PART - C**

1. **4** P110603

Sol.  $\frac{m_A \ell^2}{m_B \ell^2} = 3$

$\therefore \frac{m_A}{m_B} = 3$

$x_{CM} = \frac{m_B \ell}{m_A + m_B} = \frac{\ell}{4}$

2. **8** P110502

Sol.  $F \cdot x - \mu m_1 g x - \frac{1}{2} k x^2 = 0$

$kx = \mu m_2 g$  for just shifting  $m_2$

$F \cdot x - \mu m_1 g x - \frac{1}{2} \mu m_2 g x = 0$

$F = \mu \left( m_1 + \frac{m_2}{2} \right) g = 0.4 \left( 1 + \frac{2}{2} \right) (10) = 8N$

3. **2** P120410

Sol. At any time length of each wire =  $l - 2vt$

Induced emf =  $4 B v (l - 2vt)$

Induced current =  $\frac{4Bv(l - 2vt)}{4\lambda(l - 2vt)} = \frac{Bv}{\lambda}$ ,  $F = B \left( \frac{Bv}{\lambda} \right) (l - 2vt) = \frac{B^2 v}{\lambda} (l - 2vt)$

$= \frac{(2)^2 \times 5}{0.5} (15 - 2 \times 5 \times 1) = 200 N$

4. **3** P120306

Sol. Initially the rod will be in equilibrium if

$2T_o = Mg$  with  $T_o = kx_o$  ... (i)

when the current  $I$  is passed through the rod, it will experience a force

$F = BIL$  vertically up,

In equilibriums

$2T + BIL = Mg$  with  $T = kx$  ... (ii)

from (i) & (ii)

$\frac{T}{T_o} = \frac{Mg - BIL}{Mg}$  i.c.  $\frac{x}{x_o} = 1 - \frac{BIL}{Mg}$

or,  $B = \frac{Mg(x_o - x)}{I L x_o}$

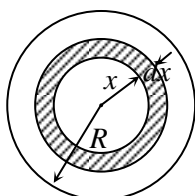
Putting the values we get  $B = 1.5 \times 10^{-2} T$ .

5. **1** P120413

Sol.  $d\phi = (2\pi x dx) k x t^2$

$\phi = \frac{2}{3} k t^2 \pi x^3$

$\frac{d\phi}{dt} = \frac{4k\pi t x^3}{3}$



$$E2\pi x = \frac{4\pi ktx^3}{3} ; \quad E = \frac{2}{3} ktx^2 ; \quad d\tau = \left(\frac{2}{3} ktx^2\right) \frac{Q}{\pi R^2} (2\pi x dx)x$$

$$\int d\tau = \frac{4}{3} \frac{ktQ}{R^2} \int_0^R x^4 dx \Rightarrow \tau = \frac{4}{3} \frac{ktQ}{R^2} \frac{R^5}{5}$$

At t = 15sec,  $\tau = 1$  N-m

6. 4 P120401

Sol. Let any instant of time, velocity of the rod is v towards right.

The current in the circuit is i. In the figure,

$$V_a - V_b = V_d - V_c$$

i.e.  $Ldi = Bldx$

Integrating, we get  $Li = Blx$

Magnetic force on the rod at this instant is

$$F_m = i l B = \frac{B^2 l^2}{L} x \quad \dots (i)$$

Since, this force is in opposite direction of  $\vec{v}$ , so from Newton's second law we can write,

$$m \left( \frac{d^2 x}{dt^2} \right) = - \frac{B^2 l^2}{L} x$$

Comparing this with equation of SHM, i.e.

$$\frac{d^2 x}{dt^2} = -\omega^2 x \quad \dots (ii)$$

We have,  $\omega = \frac{Bl}{\sqrt{mL}}$

$$\text{So } T = \frac{2\pi}{\omega} = 2\pi \frac{\sqrt{mL}}{Bl} = 2\pi \frac{\sqrt{8 \times 2}}{\pi \times 2} = 4 \text{ sec.}$$

